

FRP-RC Design - Part 3b

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Design of concrete structures internally reinforced with FRP bars

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Course Description

Fiber-reinforced polymer (FRP) materials have emerged as an alternative for producing reinforcing bars for concrete structures. Due to other differences in the physical and mechanical behavior of FRP materials versus steel, unique guidance on the engineering and construction of concrete structures reinforced with FRP bars is necessary.



Learning Objectives

- Understand the mechanical properties of FRP bars
- Describe the behavior of FRP bars
- Describe the design assumptions
- Describe the flexural/shear/compression design procedures of concrete members internally reinforced with FRP bars
- Describe the use of internal FRP bars for serviceability & durability design including long-term deflection
- Review the procedure for determining the development and splice length of FRP bars.

Content of the Course

FRP-RC Design - Part 1, (50 min.)

This session will introduce concepts for reinforced concrete design with FRP rebar. Topics will address:

- Recent developments and applications
- Different bar and fiber types;
- Design and construction resources;
- Standards and policies;

FRP-RC Design - Part 2, (50 min.)

This session will introduce Basalt FRP rebar that is being standardized under FHWA funded project *STIC-0004-00A* with extended FDOT research under BE694, and provide training on the flexural design of beams, slabs, and columns for:

- Design Assumptions and Material Properties
- Ultimate capacity and rebar development length under strength limit states;
- Crack width, sustained load resistance, and deflection under service limit state;



Content of the Seminar

BFRP-RC Design - Part 3, (50 min.)

This session continues with Basalt FRP rebar from Part II, covering shear and axial design of columns at the strength limit states for:

- Ultimate capacity Flexural behavior (Session 3a);
- Shear resistance of beams and slabs (Session 3b);
- Fatigue resistance under the Fatigue limit state
- Axial Resistance of columns;
- Combined axial and flexure loading.

FRP-RC Design - Part IV (Not included at FTS - for future training):

This session continues with FRP rebar from Part III, covering detailing and plans preparation:

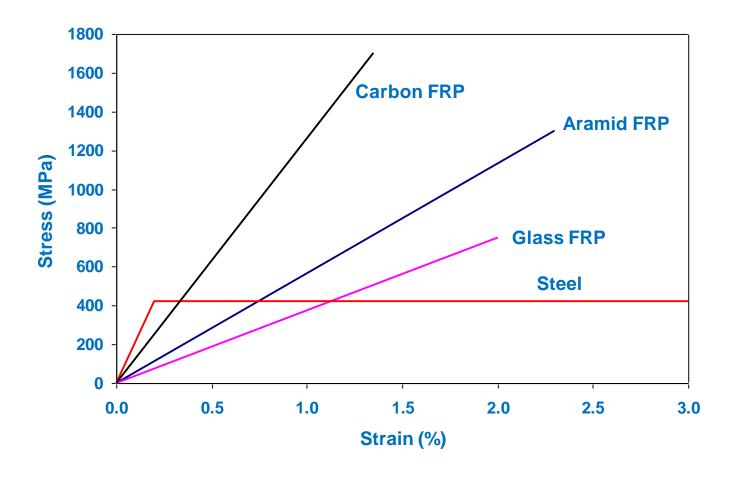
- Minimum Shrinkage and Temperature Reinforcing
- Bar Bends and Splicing
- Reinforcing Bar Lists
- General Notes & Specifications



Session 4: (1:30 pm - 2:30 pm)
Shear behaviour

- Design philosophy
- - Shear strength
- - Design examples

Stress-Strain Relationships for FRP Bars



Shear Strength of FRP Reinforced Members

- FRP has a relatively low modulus of elasticity
- FRP has a high tensile strength and no yielding point
- Tensile strength of a bent portion of an FRP bar is significantly lower than a straight portion
- FRP has low dowel resistance

Shear Strength of FRP Reinforced Members

- Concrete reinforced with FRP has a lower shear strength than concrete with steel reinforcement
 - Increased crack width → Less aggregate interlocking
 - Small compressive → Less concrete resistance in the zone compressive

Most of the design codes and design guidelines recommend the following simplified approach for shear design:

$$V_n = V_{cf} + V_{sf} + V_p$$

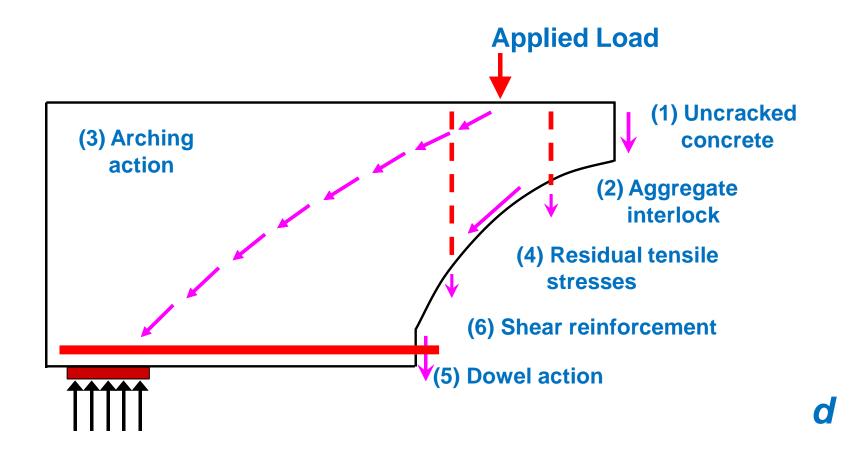
where

 V_n = nominal shear strength

 V_{cf} = concrete contribution to shear strength

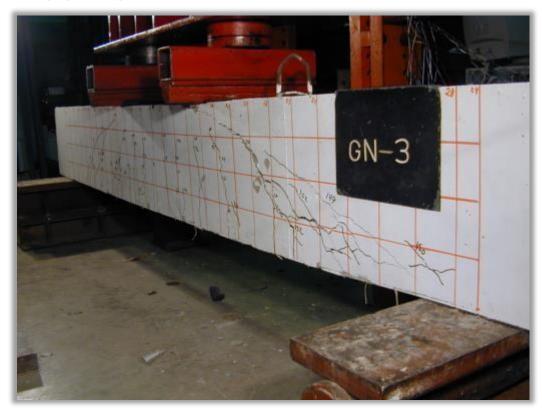
 V_{sf} = shear reinforcement contribution to shear strength

 V_p = prestressing resisting component



Shear Behaviour of FRP RC Beams





Beam CN-3

Beam GN-3

Diagonal tension failure mode



Size Effect





Beam B1-1

Beam B1-2

Diagonal Tension Failure Mode







Shear Failure of SC-9.5-2 (CFRP @ d/2)









Reinforcing Cage and Concrete Casting









Curing and transportation

Shear Behaviour of FRP RC Beams





GFRP-Cages

Shear Behaviour of FRP RC Beams; GFRP & CFRP Stirrups







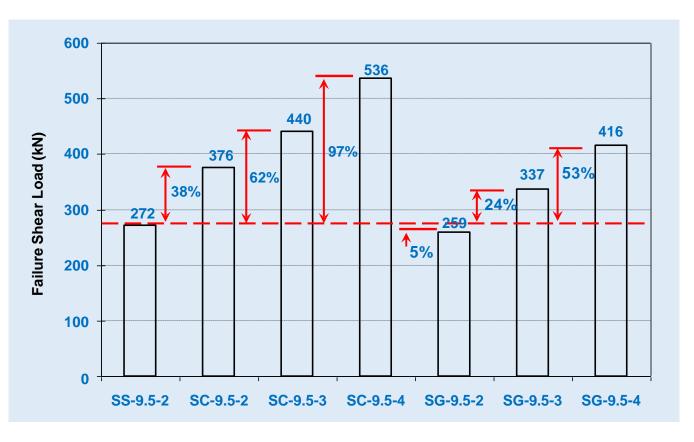
CFRP Stirrups



Shear Failure of SC-9.5-3 (CFRP @ d/3)



Shear Failure of SS-9.5-2 (Steel @ d/2)



Shear design is similar to the simplified method of CSA A23.3-14, i.e.

$$V_r \ge V_c + V_{s,F}$$

V_c accounts for

- Shear resistance of uncracked concrete
- Aggregate interlock
- Dowel action of the longitudinal reinforcement
- Arching action

 $V_{s,F}$ = Shear carried by the FRP shear reinforcement

For FRP Stirrups

$$V_r = V_c + V_{s,F}$$

For Steel Stirrups

$$V_r = V_c + V_{s,F}$$

However, V_r shall not exceed

$$V_{r,\text{max}} = 0.22 \varphi_c f_c b_w d_v + 0.5 V_p + \left[\frac{M_{dc} V_f}{M} \right]$$

If the member <u>effective depth</u> does <u>not exceed 300 mm</u> and there is no axial load:

$$V_{c} = 0.05 \lambda \varphi_{c} k_{m} k_{r} \left(f_{c}^{'}\right)^{1/3} b_{w} d_{v}$$

$$where$$

$$k_{m} = \sqrt{\frac{V_{f} d}{M_{f}}} \le 1$$

$$k_{r} = 1 + (E_{F} \rho_{Fw})^{1/3}$$

BUT
$$V_c \le 0.22 \varphi_c \sqrt{f'_c} b_w d_v$$

$$V_c \ge 0.11 \varphi_c \sqrt{f'_c} b_w d_v$$

$$f'_c \le 60 MPa$$

or if the member <u>effective depth exceeds 300 mm</u> and transverse shear reinforcements are equal or greater to $A_{v,min}$ (Clause 8.4.4.8)

To account for size effect, for sections with an effective depth greater than 300mm and with less transverse reinforcement than $A_{v,min}$

$$V_{c} = 0.05 \lambda \varphi_{c} k_{m} k_{r} k_{s} \left(f_{c}^{'}\right)^{1/3} b_{w} d_{v}$$
where
$$k_{s} = \frac{750}{450 + d} \le 1$$

Shear Carried by Transverse Reinforcement

For Members with FRP Transverse Reinforcement

$$V_{s,F} = \frac{0.4 \varphi_F A_{Fv} f_{Fu} d_v}{s} \cot \theta$$

For Members with Steel Transverse Reinforcement

$$V_{s,s} = \frac{\varphi_s A_v f_y d_v}{s} \cot \theta$$

f_{Fu} shall not be greater than 0.005E_F

- Minimum Shear Reinforcement
 - A minimum area of shear reinforcement shall be provided in all regions of flexural members where

$$V_f > 0.5V_c + \Phi_F V_{p,} \text{ or } T_f > 0.5T_{cr}.$$

This requirement may be waived for:

- Slabs and footings
- Concrete joist construction
- •Beams with total depth not greater than 250 mm
- •Beams cast integrally with slabs where overall depth is not greater than one-half the width of the web or 600 mm.

- Minimum Shear Reinforcement
 - The minimum are of FRP shear reinforcement shall be such that

$$A_{vF} = 0.07 \sqrt{f_c'} \frac{b_w s}{0.4 f_{Fu}}$$

f_{Fu} shall not be greater than 1200MPa or 0.005E_F.

Shear resistance is calculated as:

$$V_r = V_c + V_{sf} \le 0.25 \phi_c f_c b_w d_{long}$$

Where
$$V_c = 2.5 \beta \phi_c f_{cr} b_v d_{long}$$

$$V_{sf} = \frac{\phi_{frp} A_{fv} f_{fv} d_{long} \cot \theta}{s}$$

$$d_{long} = 0.72h$$
 or 0.9d

Simplified Method

For sections with at least minimum shear reinforcement

$$\theta = 42^{\circ}$$
 $\beta = 0.18$

For sections without minimum shear reinforcement

$$\beta = \frac{42^{\circ}}{230}$$

$$\beta = \frac{230}{1000 + d_{long}}$$

General Method

$$\beta = \frac{0.4}{\left(1 + 1500 \, \varepsilon_{x}\right)} \cdot \frac{1300}{\left(1000 + S_{ze}\right)}$$

$$\theta = (29 + 7000 \varepsilon_x)(0.88 + S_{ze} / 2500)$$

$$S_{ze} = 300mm$$

$$\varepsilon_{x} = \frac{\left(M_{f}/d_{long}\right) + V_{f}}{2 E_{fl} A_{fl}}$$

The stress in FRP stirrup, f_{fv}, is calculated as:

$$f_{fV} = 0.004 E_{fV} \le f_{bend}$$

$$f_{bend} = \left(0.3 + 0.05 \frac{r_b}{d_b}\right) f_{fuv} \le f_{fuv}$$

Minimum Shear Reinforcement

$$A_{fv,\text{min}} = 0.06\sqrt{f_c'} \frac{b_w s}{f_{fv}}$$

$$s \le 0.75 d_v$$
 or $600mm$ if $V_f < 0.1 \phi_c f_c b_w d_{long}$

$$s \le 0.33 \, d_v \text{ or } 300 \, mm \text{ if } V_f > 0.1 \phi_c f_c \, b_w \, d_{long}$$

Session 3b: Shear Design Example (CSA-S806)

A normal density concrete beam needs to carry a dead load of 17.5 N/mm and live load of 20 N/mm over a 6000 mm single span in addition to its own self-weight. Information on the beam cross-section and longitudinal reinforcement is provided below. Determine the required amount of shear reinforcement using GFRP ISOROD Stirrups.

GIVEN:

Dimensions: b = 350 mm d = 515 mm h = 600 mm L = 6000 mm Concrete Strength: $f'_c = 40 \text{ MPa}$ Flexural Reinforcement: $A_{frp} = 1131 \text{ mm}^2$ [2 Layers] $E_{frp} = 147 \text{ GPa}$, d_v

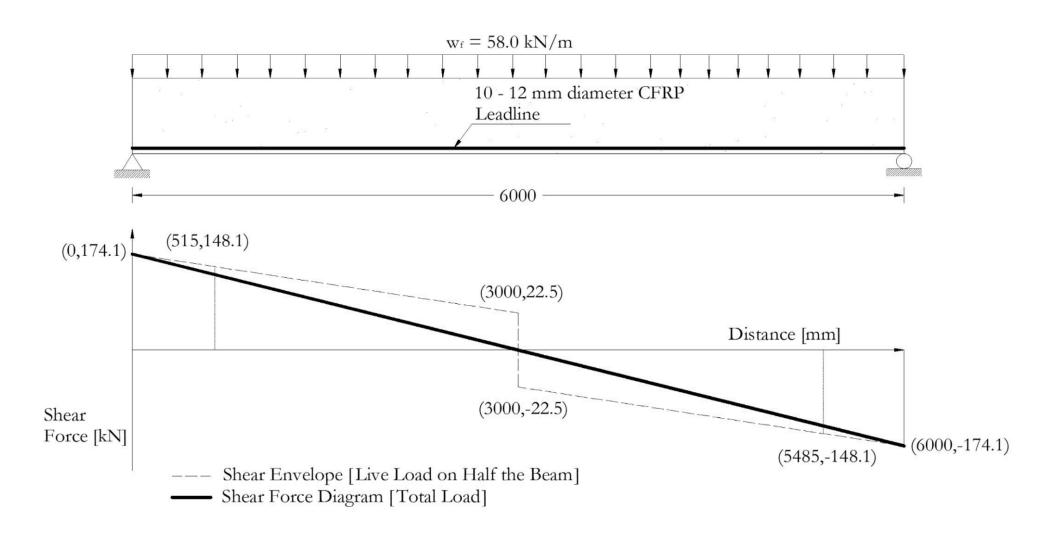
= 464 mmShear Reinforcement: $f_{frpv} = 770 \text{ MPa}$ $E_{frpv} = 43.9 \text{ GPa}$

Section Properties: $M_R = 418.9 \times 10^6 \text{ N} \cdot \text{mm}$ $M_{\text{ser}} = 149 \times 10^6 \text{ N} \cdot \text{mm}$ $w_{\text{ser}} = 33$

N/mm

 $V_{ser} = 99.3 \times 10^3 \text{ N [Support]}$





CAN/CSA-S6-14 Design Code

Factored Load

```
w_u = 1.2 w_{DL} + 1.7 w_{LL}

w_u = 1.2 (17.5+5 kN/m) + 1.7 (20 kN/m)

w_u = 61 kN/m
```

CAN/CSA-S6-14 Design Code

Shear and moment at critical section:

(at a distance d_{long} away from the support; d_{long}=463.5 mm)

$$d_{long}$$
= 0.9 d =0.9x515=463.5 mm
 V_f = w_u L / 2- w_u d_v
 V_f = 61 x 6.0 /2 - 61 x 0.4635 = 154.7 kN
 M_f =61x3.0x0.4635 - 61x(0.4635)²/2=78.3 kN.m

CAN/CSA-S6-14 Design Code V_{cf}:

$$V_c = 2.5 \beta \phi_c f_{cr} b_v d_{long}$$

$$f_{cr} = 0.4\sqrt{f_c'} = 0.4\sqrt{40} = 2.53 \, MPa < 3.2 \, MPa$$

$$\beta = \frac{0.4}{(1+1500 \,\varepsilon_{x})} \cdot \frac{1300}{(1000 + S_{ze})} \qquad S_{ze} = 300 mm$$

$$\varepsilon_{x} = \frac{\left(M_{f}/d_{long}\right) + V_{f}}{2 E_{ff} A_{ff}} = \frac{\left(78.3/0.515\right) + 154.7}{2 \times 1131 \times 147000} \times 1000 = 0.001 < 0.003$$

$$\beta = \frac{0.4}{\left(1 + 1500 \times 0.001\right)} \cdot \frac{1300}{\left(1000 + 300\right)} = 0.267$$

CAN/CSA-S6-14 Design Code

$$V_c = 2.5 \times 0.267 \times 0.75 \times 2.53 \times 350 \times 463.5 \times 10^{-3} = 205.47 \text{ kN}$$

$$s_{\text{max}} = \frac{A_{f_V} f_{f_V}}{0.06 \sqrt{f_c'} b_w}$$

$$s_{\text{max}} = \frac{2 \times 71.26 \times 0.004 \times 43900}{0.06 \sqrt{40} \times 350} = 188 \text{mm}$$

Use GFRP No. 3 stirrups with s=180 mm

CAN/CSA-S806-12 Code

Factored Load

```
w_{sw} = 0.35 \times 0.60 \times 24 = 5 \text{ kN/m}
w_u = 1.25 \text{ w}_{DL} + 1.5 \text{ w}_{LL}
w_u = 1.25 (17.5 + 5 \text{ kN/m}) + 1.5 (20 \text{ kN/m})
w_{tt} = 58 \text{ kN/m}
```

CAN/CSA-S806-12 Code

Shear and moment at critical section:

(at a distance d_v away from the support; d_v=463.5 mm)

$$V_u = w_u L / 2 - w_u d$$
 $V_u = 58 \times 6.0 / 2 - 58 \times 0.4635 = 147.12 \text{ kN}$
 $M_u = w_u (L/2) d - w_u d^2/2$
 $M_u = 58 \times 3.0 \times 0.4635 - 58 \times 0.4635^2/2$
 $= 74.4 \text{ kN.m}$

CAN/CSA-S806-12 Code V_{cf}:

$$V_{cf} = 0.05 \ \lambda \ \phi_c \ k_m \ k_r \left(f_c' \right)^{1/3} b_w d_v$$

$$d_v = 0.7 \times 600 = 420 mm \ or \ 0.9 \times 515 = 463.5 mm$$

$$d_v = 463.5 mm$$

$$\rho_{fw} = \frac{1131}{350 \times 515} = 0.0063$$

$$k_m = 1 + \left(147000 \times 0.0063 \right)^{1/3} = 10.75$$

$$k_r = \sqrt{\frac{V_u}{M_u}} d = \sqrt{\frac{147.12 \times 0.515}{74.4}} = 1.0 \ ok$$

$$k_a = 1.0$$

$$V_{cf} = 0.05 \times 1 \times 0.6 \times 10.75 \times 1.0 \times (40)^{1/3} \times 350 \times 463.5 \times 1.0 \times 10^{-3}$$

= 178.9 kN

CAN/CSA-S806-12 Code

$$V_{cf} > V_f$$

Use minimum shear reinforcement

$$f_{fu} \le 0.005E_f = 0.005 \times 43900 = 219.5 < 1200 MPa$$
 ok

$$A_{sf} = 0.07 \sqrt{f_c'} \frac{b_w s}{0.4 f_{fu}}$$

GFRP No. 3
$$2 \times 71.26 = 0.07\sqrt{40} \frac{350 \times s}{0.4 \times 219.5}$$
 $s = 80 \text{ mm}$

GFRP No. 4
$$2 \times 126.68 = 0.07 \sqrt{40} \frac{350 \times s}{0.4 \times 219.5}$$
 $s = 143 mm$

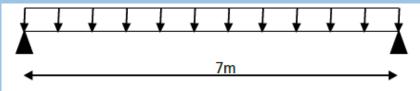
Use GFRP stirrups No.4 @140mm

Additional Shear Design of Beam Reinforced with GFRP Bars According to *CSA S806-12*

Loads:

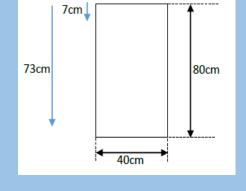
Dead load (D.L) = 85 kN/m

Live load (L.L) = 40 kN/m



Service limit state $(W_{s,l,s}) = 85 + 40 = 125 \text{ kN/m}$

Ultimate limit state $(W_{u,l,s}) = 1.25 * 85 + 1.5 * 40 = 166.25 \text{ kN/m}$



	S.L.S	U.L.S
V = W L / 2 (kN)	<i>437.50</i>	<i>581.88</i>
$M = W L^2/8$ (kN.m)	765.63	1018.28

Mechanical Properties

Concrete

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f_c'=30 MPa
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GFRP (Grade III)

GFRP straight bar #8 (25 mm-diameter)

 $A_f = 506.7 \,\text{mm}^2$; $E_f = 66.4 \,\text{GPa}$; Guaranteed tensile strength (f_{fu}) = 1000 MPa.

GFRP bent bar #3 (10 mm-diameter)

 $A_f = 71.3 \text{ mm}^2$; $E_f = 50 \text{ GPa}$; Guaranteed tensile strength $(f_{fu}) = 460 \text{ MPa}$.

Session 3b: Shear Design Example (CSA-S806) Notes and Assumptions

- Concrete cover = 30 mm or 2d_b (Clause 8.2.3).
- Assume exterior exposure of the beam for crack control.
- Minimum clear spacing between longitudinal bars
 = 20 mm (for vertical and horizontal spacing).
- Concrete resistance factor $(\varphi_c) = 0.65$ (Clause 6.5.3.2).
- GFRP resistance factor (ϕ_{FRP}) = 0.75 (Clause 7.1.6.3).
- Bond dependent coefficient (k_b) = 0.8 (sand-coated bars)

Design Steps

Design for shear force

- Calculate concrete contribution.
- Calculate GFRP stirrups contribution

Shear Design

Shear force at distance d_v

Clause

8.4.4.2

 d_v = effective shear depth, taken as the greater of 0.9d or

0.72h

 $d_v = Max (0.9*716.6 \text{ or } 0.72*800) = 644.97 \text{ mm}$

 $V_{\text{design U.L.S}} = 581.875 - 166.25 * 0.645 = 474.65 \text{ kN}$

 $V_r = V_c + V_{sF}$

Equation 8.14

 $V_{r,max} = 0.22 \phi_c f'_c b_w d_v$

Equation 8.16

Shear Design

Concrete contribution (Clause 8.4.4.2)

$$0.11\varphi_{c}\sqrt{f_{c}'}b_{w}d_{v} \leq V_{c} = 0.05\lambda\varphi_{c}k_{m}k_{r}(f'_{c})^{1/3}b_{w}d_{v}k_{s}$$

$$\leq 0.22\varphi_{c}\sqrt{f_{c}'}b_{w}d_{v}$$

$$M_{f} = 581.875 * 0.645 - 166.25 * 0.645^{2}/2 = 340.72 \text{ kN. m}$$

$$k_{m} = \sqrt{\frac{V_{f}d}{M_{f}}} \leq 1.0 \rightarrow k_{m} = \sqrt{\frac{474.65x716.6}{340.72x1000}} = 0.999$$

$$k_{r} = 1 + (E_{f}\rho_{Fw})^{1/3} \rightarrow k_{r} = 1 + (66400 * 0.0283)^{1/3} = 13.34$$

$$k_{a} = \frac{2.5}{\frac{M_{f}}{V_{f}d}} \rightarrow k_{a} = 1 + \frac{2.5}{\frac{340.72 * 1000}{474.65x716.6}} = 2.496$$

Shear Design

Concrete contribution (Clause 8.4.4.2)

$$k_s = \frac{750}{450 + d} \rightarrow k_s = \frac{750}{450 + 716.6} = 0.643$$

$$0.11 \varphi_c \sqrt{f_c'} b_w d_v = 0.11 * 0.65 * \sqrt{30} * 400 * 644.97 = 101.03 \, kN$$

$$V_c = 0.05 * 0.65 * 0.999 * 13.34 * 30^{1/3} * 0.643 * 400 * 644.97$$

$$* 2.496 = 557.1 \, kN$$

$$0.22 \varphi_c \sqrt{f_c'} b_w d_v = 0.22 * 0.65 \sqrt{30} * 400 * 644.97 = 202.07 \, kN$$

$$V_c = 202.07 \, kN$$

Shear Design

GFRP stirrups contribution

$$V_{SF} = \frac{\varphi_F A_{Fv} f_{Fu} d_v}{s} \cot \theta$$

$$\theta = 30^{\circ} + 7000\varepsilon_l$$

$$\varepsilon_l = \frac{\frac{M_f}{d_v} + V_f}{2(E_f A_f)}$$

$$\varepsilon_l = \frac{\frac{340.72 * 106}{644.97} + 474.65 * 103}{2(66400 * 8107.2)} = 0.00093$$

Equation 8-22

Equation 8-24

Equation 8-25

Shear Design

GFRP stirrups contribution

$$\theta = 30^{\circ} + 7000 * 0.00093 = 36.52^{\circ}$$

Assuming stirrups #3 each 150 mm c.c

$$V_{SF} = \frac{0.75 * (2 * 71.3) * 460 * 644.97}{150} \cot 36.52 \circ = 285.66 \text{ kN}$$

$$V_r = V_c + V_{SF} = 202.07 + 285.66 = 487.73 \ kN > V_r$$

Session 1: Introduction

End of Session

Questions

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